

Objectives

- Convert between decimal notation and percent notation.
- Solve problems involving percent.

Definition 1. *Percent means per one hundred. We use % to denote percent.*

For instance, 23% means 23 per 100, 23% is the ratio of 23 to 100, or $\frac{23}{100}$.

Also, $1\% = \frac{1}{100} = 0.01$; and $100\% = \frac{100}{100} = 1$.

Write Percents as Decimals

To write a percent as a decimal, replace the % symbol with its decimal equivalent, 0.01; then multiply. This is equivalent to removing the % symbol and moving the decimal point of the number left of the % *two places to the left*.

1. Write each percent as a decimal.

- a) 39% b) 100% c) 3.14% d) 2.7% e) 0.74%

Converting Decimals to Percents

To write a decimal as a percent, multiply by 100%. This is equivalent to moving the decimal point 2 places to the right and attaching a % symbol.

2. Write each decimal as a percent.

- a) 0.52 b) 0.017 c) 0.73 d) 1.20 e) 0.2344

Recognizing key words in a percent problem is helpful in writing the problem as an equation. Three key words in the statement of a percent problem and their meanings are:

of means **multiplication** (\cdot)

is means **equal** ($=$)

what (or *some equivalent*) means **the unknown number**

Example 1: Translate this phrase to an equation: **3 is what percent of 12?**

Solution: 3 is what percent of 12?

$$\begin{array}{ccccccc} \downarrow\downarrow & & \downarrow & & \downarrow & \downarrow & \\ 3 = & & x & & \cdot & 12 & \end{array}$$

Example 2: Translate this phrase to an equation: **3.2 is 60% of what number?**

Solution: 3.2 is 60% of what number?

$$\begin{array}{ccccccc} \downarrow & \downarrow & \downarrow & \downarrow & & \downarrow & \\ 3.2 = & 60\% \cdot & & & & x & \end{array}$$

Example 3: Translate this phrase to an equation: **What number is 20% of 0.07**

Solution: What number is 20% of 0.07?
 ↓ ↓ ↓ ↓ ↓
 x = 20% · 0.07

3. Set up an equation and solve for the unknown.

- a) What number is 25% of 90?
 - b) 95% of 400 is what number?
 - c) 63 is what percent of 45?
 - d) 0.5% of 100 is what number?
 - e) 150% of what number is 60?
 - f) 3.2 is what percent of 128?
 - g) 0.50 is what percent of 4.50?
4. During one year, Sashy's city tax included \$487 for local schools. Of this amount, \$195 went to the high school district. What percent did Sashy pay to the high school district? (Round your answer to the nearest whole number percent.)
5. If Gloria received a 5 percent raise and is now making \$22,050 a year, what was her salary before the raise? Round to the nearest dollar if necessary.
6. It is Selena's turn to leave the tip at a business dinner that cost \$287.60. If she tips 20% of that, how much of a tip did she leave?

Answers: 1a) 0.39, b) 1, c) 0.0314, d) 0.027, e) 0.0074, 2a) 52%, b) 1.7%, c) 73%, d) 120%, e) 23.44%, 3a) 22.5 b) 380, c) 140%, d) 5, e) 40, f) 2.5 4) 40%, 5) \$21,000, 6) \$57.52