

7.5 Estimating Standard D and Variance

MULTIPLE CHOICE. Choose the one alternative that best completes the statement or answers the question.

Use the given degree of confidence and sample data to find a confidence interval for the population standard deviation σ . Assume that the population has a normal distribution. Round the confidence interval limits to the same number of decimal places as the sample standard deviation.

- 1) Weights of men: 90% confidence; $n = 14$, $\bar{x} = 157.8$ lb, $s = 12.4$ lb 1) _____
 A) $9.2 \text{ lb} < \sigma < 17.4 \text{ lb}$ B) $9.5 \text{ lb} < \sigma < 18.4 \text{ lb}$
 C) $10.0 \text{ lb} < \sigma < 2.7 \text{ lb}$ D) $9.7 \text{ lb} < \sigma < 16.0 \text{ lb}$
- 2) The mean replacement time for a random sample of 20 washing machines is 10.3 years and the standard deviation is 2.7 years. Construct a 99% confidence interval for the standard deviation, σ , of the replacement times of all washing machines of this type. 2) _____
 A) $2.0 \text{ yr} < \sigma < 4.3 \text{ yr}$ B) $1.9 \text{ yr} < \sigma < 4.5 \text{ yr}$
 C) $1.8 \text{ yr} < \sigma < 5.1 \text{ yr}$ D) $1.9 \text{ yr} < \sigma < 5.7 \text{ yr}$
- 3) College students' annual earnings: 98% confidence; $n = 9$, $\bar{x} = \$4091$, $s = \$856$ 3) _____
 A) $\$674 < \sigma < \1117 B) $\$578 < \sigma < \1640
 C) $\$540 < \sigma < \1887 D) $\$520 < \sigma < \1675

Find the appropriate minimum sample size.

- 4) You want to be 95% confident that the sample variance is within 40% of the population variance. 4) _____
 A) 14 B) 11 C) 57 D) 224
- 5) You want to be 99% confident that the sample standard deviation s is within 5% of the population standard deviation. 5) _____
 A) 1336 B) 2638 C) 2434 D) 923

Use the given degree of confidence and sample data to construct a confidence interval for the population proportion p .

- 6) $n = 128$, $x = 61$; 90% confidence 6) _____
 A) $0.407 < p < 0.547$ B) $0.408 < p < 0.546$
 C) $0.404 < p < 0.550$ D) $0.403 < p < 0.551$

Use the confidence level and sample data to find a confidence interval for estimating the population μ . Round your answer to the same number of decimal places as the sample mean.

- 7) A laboratory tested 82 chicken eggs and found that the mean amount of cholesterol was 238 milligrams with $\sigma = 19.4$ milligrams. Construct a 95% confidence interval for the true mean cholesterol content, μ , of all such eggs. 7) _____
 A) $235 \text{ mg} < \mu < 243 \text{ mg}$ B) $233 \text{ mg} < \mu < 242 \text{ mg}$
 C) $233 \text{ mg} < \mu < 241 \text{ mg}$ D) $234 \text{ mg} < \mu < 242 \text{ mg}$

Use the given degree of confidence and sample data to construct a confidence interval for the population mean μ . Assume that the population has a normal distribution.

- 8) $n = 12$, $\bar{x} = 27.0$, $s = 5.9$, 99% confidence 8) _____
 A) $21.73 < \mu < 32.27$ B) $21.71 < \mu < 32.29$
 C) $21.60 < \mu < 32.40$ D) $22.37 < \mu < 31.63$

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TABLE A-4		Chi-Square (χ^2) Distribution									
		Area to the Right of the Critical Value									
Degrees of Freedom											
	0.995	0.99	0.975	0.95	0.90	0.10	0.05	0.025	0.01	0.005	
1	—	—	0.001	0.004	0.016	2.706	3.841	5.024	6.635	7.879	
2	0.010	0.020	0.051	0.103	0.211	4.605	5.991	7.378	9.210	10.597	
3	0.072	0.115	0.216	0.352	0.584	6.251	7.815	9.348	11.345	12.838	
4	0.207	0.297	0.484	0.711	1.064	7.779	9.488	11.143	13.277	14.860	
5	0.412	0.554	0.831	1.145	1.610	9.236	11.071	12.833	15.086	16.750	
6	0.676	0.872	1.237	1.635	2.204	10.645	12.592	14.449	16.812	18.548	
7	0.989	1.239	1.690	2.167	2.833	12.017	14.067	16.013	18.475	20.278	
8	1.344	1.646	2.180	2.733	3.490	13.362	15.507	17.535	20.090	21.955	
9	1.735	2.088	2.700	3.325	4.168	14.684	16.919	19.023	21.666	23.589	
10	2.156	2.558	3.247	3.940	4.865	15.987	18.307	20.483	23.209	25.188	
11	2.603	3.053	3.816	4.575	5.578	17.275	19.675	21.920	24.725	26.757	
12	3.074	3.571	4.404	5.226	6.304	18.549	21.026	23.337	26.217	28.299	
13	3.565	4.107	5.009	5.892	7.042	19.812	22.362	24.736	27.688	29.819	
14	4.075	4.660	5.629	6.571	7.790	21.064	23.685	26.119	29.141	31.319	
15	4.601	5.229	6.262	7.261	8.547	22.307	24.996	27.488	30.578	32.801	
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	28.845	32.000	34.267	
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	30.191	33.409	35.718	
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	31.526	34.805	37.156	
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	32.852	36.191	38.582	
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	34.170	37.566	39.997	
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671	35.479	38.932	41.401	
22	8.643	9.542	10.982	12.338	14.042	30.813	33.924	36.781	40.289	42.796	
23	9.260	10.196	11.689	13.091	14.848	32.007	35.172	38.076	41.638	44.181	
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	42.980	45.559	
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.314	46.928	
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	45.642	48.290	
27	11.808	12.879	14.573	16.151	18.114	36.741	40.113	43.194	46.963	49.645	
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	50.993	
29	13.121	14.257	16.047	17.708	19.768	39.087	42.557	45.722	49.588	52.336	
30	13.787	14.954	16.791	18.493	20.599	40.256	43.773	46.979	50.892	53.672	
40	20.707	22.164	24.433	26.509	29.051	51.805	55.758	59.342	63.691	66.766	
50	27.991	29.707	32.357	34.764	37.689	63.167	67.505	71.420	76.154	79.490	
60	35.534	37.485	40.482	43.188	46.459	74.397	79.082	83.298	88.379	91.952	
70	43.275	45.442	48.758	51.739	55.329	85.527	90.531	95.023	100.425	104.215	
80	51.172	53.540	57.153	60.391	64.278	96.578	101.879	106.629	112.329	116.321	
90	59.196	61.754	65.647	69.126	73.291	107.565	113.145	118.136	124.116	128.299	
100	67.328	70.065	74.222	77.929	82.358	118.498	124.342	129.561	135.807	140.169	

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Degrees of Freedom

- $n - 1$ for confidence intervals or hypothesis tests with a standard deviation or variance
- $k - 1$ for goodness-of-fit with k categories
- $(r - 1)(c - 1)$ for contingency tables with r rows and c columns
- $k - 1$ for Kruskal-Wallis test with k samples